

Find the exact value.

1. $\sin^{-1}\left(\frac{1}{2}\right)$

$\pi/6, 5\pi/6$
 $30^\circ, 150^\circ$

2. $\tan^{-1}(\sqrt{3})$

$\pi/3, 4\pi/3$
 $60^\circ, 240^\circ$

3. $\sin\left(\tan^{-1}\frac{\sqrt{3}}{3}\right)$

$\frac{1}{2}, \frac{\sqrt{3}}{2}$

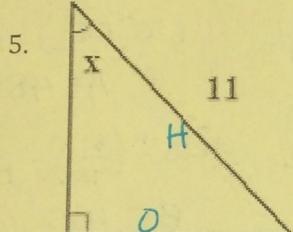
4. $\cos^{-1}\left(\sin\frac{\pi}{3}\right)$

$\pi/3, 4\pi/3$
 $60^\circ, 300^\circ$

$\frac{\pi}{6}, 11\pi/6$

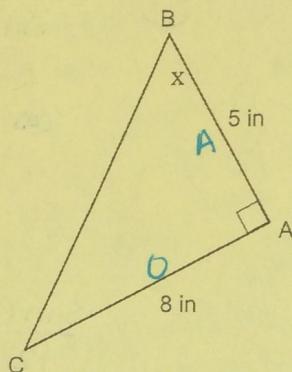
$30^\circ, 330^\circ$

Use inverse trig to find the missing angle.



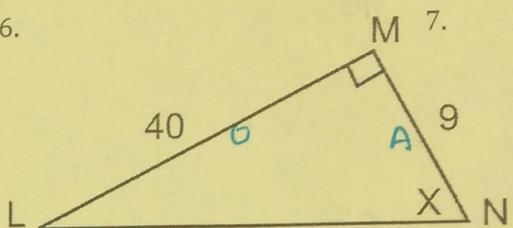
$$\sin^{-1}\left(\frac{8}{11}\right) = x$$

$x = 47^\circ$



$$\tan^{-1}\left(\frac{8}{5}\right) = x$$

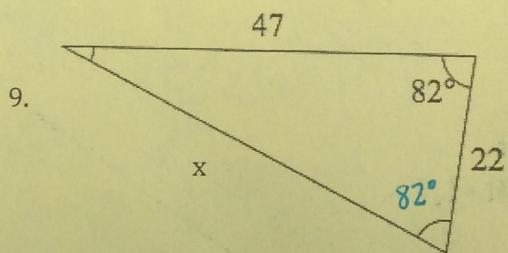
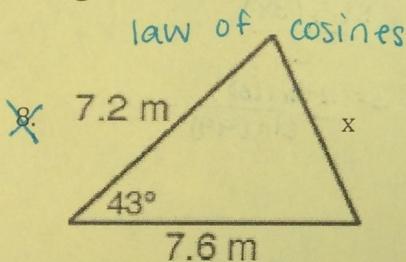
$x = 58^\circ$



$$\tan^{-1}\left(\frac{40}{9}\right) = x$$

$x = 77^\circ$

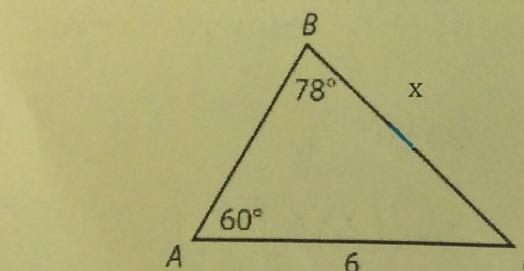
Using the law of sines, find the missing side of the triangle:



$$\frac{\sin(82)}{47} = \frac{\sin(82)}{x}$$

$x = 82$

10.



$$x = \frac{6 \sin(60)}{\sin(78)} = \boxed{5.3}$$

$$x \cdot \frac{\sin(78)}{6} = \frac{\sin(60)}{x}$$

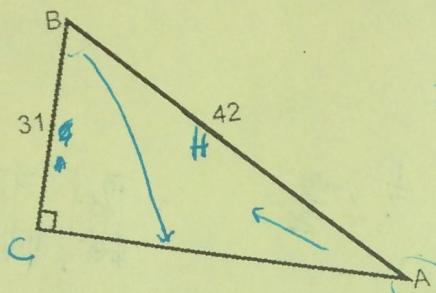
$$x \cdot \frac{x \cdot \sin(78)}{6} = \frac{\sin(60) \cdot 6}{x}$$

$$x \cdot \sin(78) = \frac{6 \cdot \sin(60)}{\sin(78)}$$

Solve the following triangles (find ALL angles and sides)

11.

$$\begin{aligned} a &= 31 \\ b &= 28.3 \\ c &= 42 \\ A &= 48^\circ \\ B &= 42^\circ \\ C &= 90 \end{aligned}$$



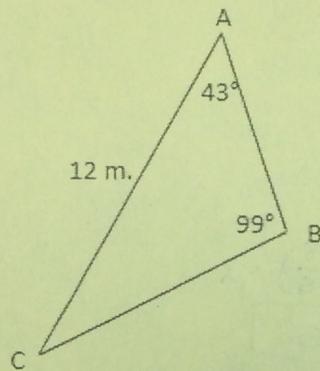
$$\begin{aligned} 31^2 + b^2 &= 42^2 \\ b^2 &= \sqrt{42^2 - 31^2} \\ b &= 28.3 \end{aligned}$$

$$\begin{aligned} \sin A &= \frac{31}{42} & \sin^{-1}\left(\frac{31}{42}\right) &= A \\ & & A &= 48^\circ \end{aligned}$$

$$\begin{aligned} \cos B &= \frac{31}{42} & \cos^{-1}\left(\frac{31}{42}\right) &= B \\ & & B &= 42^\circ \end{aligned}$$

12.

$$\begin{aligned} a &= 8.3 \\ b &= 12 \\ c &= 7.5 \\ A &= 43^\circ \\ B &= 99^\circ \\ C &= 38^\circ \end{aligned}$$



$$180 - 43 - 99 = 38$$

$$\frac{\sin(99)}{12} = \frac{\sin(43)}{a}$$

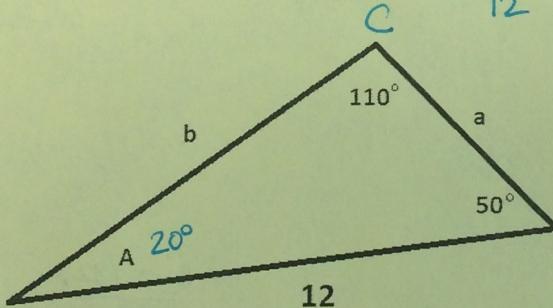
$$a = \frac{12 \sin(43)}{\sin(99)} = 8.3$$

$$\frac{\sin(99)}{12} = \frac{\sin(38)}{c}$$

$$c = \frac{12 \sin(38)}{\sin(99)} = 7.5$$

13.

$$\begin{aligned} a &= 4.4 \\ b &= 9.8 \\ c &= 12 \\ A &= 20^\circ \\ B &= 50^\circ \\ C &= 110 \end{aligned}$$

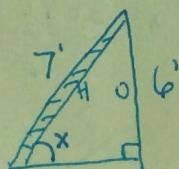


$$a = \frac{12 \cdot \sin(20)}{\sin(110)} = 4.4$$

$$b = \frac{12 \cdot \sin(50)}{\sin(110)} = \frac{9.8}{\sin(110)}$$

$$b = \frac{12 \cdot \sin(50)}{\sin(110)} = \frac{9.8}{\sin(110)} = 9.8$$

14. Jerry is hanging a poster for the upcoming spring dance. He has a ladder that is 7 feet long, and wants to hang the poster up on the wall at 6 feet high. What angle does the ladder need to make with the ground for the poster to be 6 feet high?



$$\sin(x) = \frac{6}{7}$$

$$\sin^{-1}\left(\frac{6}{7}\right) = 59^\circ$$