

Given a polynomial divisor and dividend, use long division to find the quotient and remainder.

$$1. (18x^3 - 3x^2 + x - 1) \mid (x^2 - 4)$$

$$2. (6x^4 + x^3 - 9x + 13) \mid (x^2 + 8)$$

$$\boxed{6x^2 + x - 48 \quad R: -17x + 397}$$

$$\begin{array}{r}
 x^2 + 8 \\
 \overline{)6x^4 + x^3 + 0x^2 - 9x + 13} \\
 -6x^4 - 0x^3 \\
 \hline
 x^3 - 48x^2 - 9x \\
 -x^3 - 0x^2 - 8x \\
 \hline
 -48x^2 - 17x + 13 \\
 +48x^2 + 0x + 384 \\
 \hline
 -17x + 397
 \end{array}$$

$$3. (x^3 + 25x^2 + 100x) \mid (x + 20)$$

Given a polynomial  $p(x)$ , use synthetic division to divide by  $x - a$  and obtain the quotient and the (nonzero) remainder.

$$4. (7x^3 - 4x^2 - 400x - 100) \mid (x - 8)$$

$$5. (2.5x^3 + 6x^2 - 5.5x - 10) \mid (x + 1)$$

$$\begin{array}{r}
 +8 \\
 \hline
 7 & -4 & -400 & -100 \\
 + \downarrow & 56 & 416 & 128 \\
 \hline
 7 & 52 & 16 & \underline{128}
 \end{array}$$

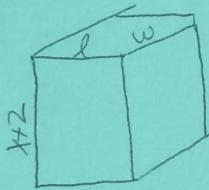
$$\boxed{7x^2 + 52x + 16 \quad R: 28}$$

6.  $(3x^3 - 11x^2 - 56x - 50) \div (x + 4)$

$$\begin{array}{r} -4 \\ \underline{-} \quad | \quad 3 \quad -11 \quad -56 \quad -50 \\ \quad \downarrow \quad \quad -12 \quad 92 \quad -144 \\ \hline 3 \quad -23 \quad 36 \quad \boxed{-194} \end{array}$$

$$3x^2 - 23x + 36 \quad R: -194$$

7. Given that the height of a rectangular prism is  $x+2$  and the volume is  $x^3 - x^2 - 6x$ , write an expression that represents the area of the top face of the prism.



$$V = l \cdot w \cdot h = x^3 - x^2 - 6x$$

$$l \cdot w \cdot (x+2) = x^3 - x^2 - 6x$$

$$l \cdot w = (x^3 - x^2 - 6x) \div (x+2) = ?$$

You finish it!

8. Explain the error: Two students used synthetic division to divide  $3x^3 - 2x - 8$  by  $x - 2$ . Determine which solution is correct. Find the error in the other solution.

A.	B.
$\begin{array}{r} 2   \quad 3 \quad 0 \quad -2 \quad -8 \\ \quad \quad 6 \quad 12 \quad 20 \\ \hline \quad 3 \quad 6 \quad 10 \quad 12 \end{array}$	$\begin{array}{r} 2   \quad 3 \quad 0 \quad -2 \quad -8 \\ \quad \quad -6 \quad 12 \quad -20 \\ \hline \quad 3 \quad -6 \quad 10 \quad -28 \end{array}$

## Review

Graph the function  $f(x) = \begin{cases} (x+2)^2, & x < 0 \\ -1, & x > 0 \end{cases}$

