

Given a polynomial divisor and dividend, use long division to find the quotient and remainder.

1. $(x^2 + 14x + 38) \div (x + 8)$

2. $(x^2 - 74) \div (x - 8)$

$$\begin{array}{r} \boxed{x + 8 \quad R: -10} \\ x-8 \overline{) x^2 + 0x - 74} \\ \underline{-x^2 + 8x} \\ 8x - 74 \\ \underline{-8x + 64} \\ -10 \end{array}$$

3. $(x^3 + 7x^2 + 14x + 3) \div (x + 2)$

4. $(x^3 - 13x^2 + 40x + 18) \div (x - 7)$

$$\begin{array}{r} \boxed{x^2 + 5x + 4 \quad R: -5} \\ x+2 \overline{) x^3 + 7x^2 + 14x + 3} \\ \underline{-x^3 + 2x^2} \\ 5x^2 + 14x \\ \underline{-5x^2 + 10x} \\ 4x + 3 \\ \underline{-4x + 8} \\ -5 \end{array}$$

5. $(3x^3 + 34x^2 + 89x + 75) \div (x + 8)$

6. $(8x^3 - 55x^2 + 44x - 12) \div (x - 6)$

$$\begin{array}{r} \boxed{8x^2 - 7x + 2 \quad R: 0} \\ x-6 \overline{) 8x^3 - 55x^2 + 44x - 12} \\ \underline{-8x^3 + 48x^2} \\ -7x^2 + 44x \\ \underline{+ 7x^2 - 42x} \\ 2x - 12 \\ \underline{-2x + 12} \\ 0 \end{array}$$

Given a polynomial $p(x)$, use synthetic division to divide by $x - a$ and obtain the quotient and the (nonzero) remainder. Write the result in the form $p(x) = (x - a)(\text{quotient}) + \text{remainder}$.

7. $(7x^3 - 4x^2 - 400x - 100) \div (x - 8)$

8. $(8x^4 - 28.5x^2 - 9x + 10) \div (x + 0.25)$

$$\begin{array}{r|rrrrrr} -0.25 & 8 & 0 & -28.5 & -9 & 10 \\ & + \downarrow & -2 & 0.5 & 7 & 0.5 \\ \hline & 8 & -2 & -28 & -2 & \underline{10.5} \\ & & & & & R \end{array}$$

$8x^3 - 2x^2 - 28x - 2 \quad R: 10.5$

9. $(2.5x^3 + 6x^2 - 5.5x - 10) \div (x + 1)$

10. $(3x^3 - 11x^2 - 56x - 50) \div (3x + 4)$

$$\begin{array}{r|rrrr} -1 & 2.5 & 6 & -5.5 & -10 \\ & + \downarrow & -2.5 & -3.5 & 9 \\ \hline & 2.5 & 3.5 & -9 & -1 \end{array}$$

$2.5x^2 + 3.5x - 9 \quad R: -1$

11. $(x^3 - 13x^2 + 40x + 18) \div (x - 7)$

12. $(x^3 + 6x^2 + 9x - 5) \div (x + 1)$

$$\begin{array}{r|rrrr} -1 & 1 & 6 & 9 & -5 \\ & + \downarrow & -1 & -5 & -4 \\ \hline & 1 & 5 & 4 & \underline{-9} \end{array}$$

$x^2 + 5x + 4 \quad R: -9$

13. Explain the error: Two students used synthetic division to divide $3x^3 - 2x - 8$ by $x - 2$. Determine which solution is correct. Find the error in the other solution.

A.	B.
$\begin{array}{r rrrr} 2 & 3 & 0 & -2 & -8 \\ & & 6 & 12 & 20 \\ \hline & 3 & 6 & 10 & 12 \end{array}$	$\begin{array}{r rrrr} 2 & 3 & 0 & -2 & -8 \\ & & -6 & 12 & -20 \\ \hline & 3 & -6 & 10 & -28 \end{array}$

Try it yourself!
Which is right?
Why is the other one wrong?