

Graphing Polynomials

Use a graphing calculator to graph the polynomial function. Then use the graph to determine the function's domain, range, and end behavior. (Use interval notation for the domain and range.)

1. $f(x) = x^7$

Domain: $(-\infty, \infty)$ Range: $(-\infty, \infty)$ End Behavior: $\downarrow \uparrow$ as $x \rightarrow -\infty, f(x) \rightarrow -\infty$ as $x \rightarrow \infty, f(x) \rightarrow \infty$

2. $f(x) = -x^9$

3. $f(x) = x^{10}$

Domain: $(-\infty, \infty)$ Range: $[0, \infty)$

4. $f(x) = -x^4$

Use a graphing calculator to graph the function. Then use the graph to state the zeros and multiplicity of each zero.

5. $f(x) = x(x+1)(x+3)$

| Zero | Multiplicity | Intersection |
|------|--------------|--------------|
| 0 | 1 | straight |
| -1 | 1 | straight |
| -3 | 1 | straight |

6. $f(x) = (x+1)^2(x-1)(x-2)$

| Zero | Multiplicity | Intersection |
|------|--------------|--------------|
| | | |
| | | |
| | | |

7. $f(x) = -x(x-2)^2$

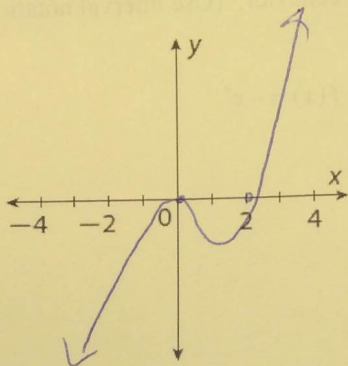
| Zero | Multiplicity | Intersection |
|------|--------------|--------------|
| 0 | 1 | straight |
| 2 | 2 | tangent |
| | | |

8. $f(x) = -(x-1)(x+2)^3$

| Zero | Multiplicity | Intersection |
|------|--------------|--------------|
| | | |
| | | |
| | | |

Sketch a graph of the polynomial function.

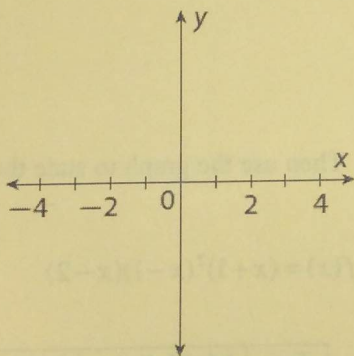
9. $f(x) = x^2(x - 2)$



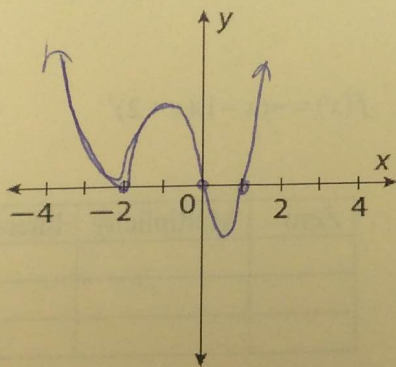
zeros: 0, 2
 ↑ tangent
 ↖ straight

EB: ↓↑

10. $f(x) = -(x + 1)(x - 2)(x - 3)$



11. $f(x) = x(x + 2)^2(x - 1)$

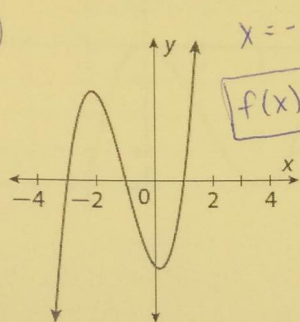


zeros: 0, -2, 1
 ↑ straight
 ↑ tangent
 ↖ straight

EB: ↑↑

Write a cubic function in intercept form for the given graph, whose x -intercepts are integers. Assume that the constant factor a is either 1 or -1 .

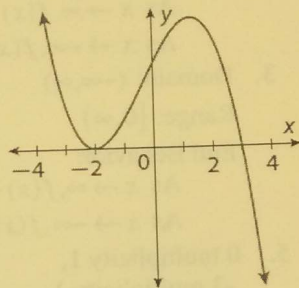
14.



$x = -3, -1, 1$

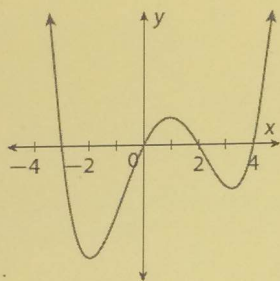
$$f(x) = (x+3)(x+1)(x-1)$$

15.

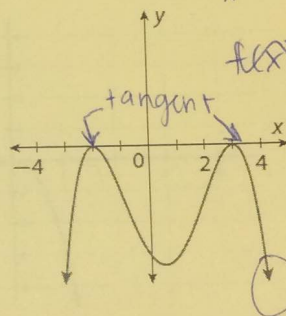


Write a quartic function in intercept form for the given graph, whose x -intercepts are integers. Assume that the constant factor a is either 1 or -1 .

16.



17.

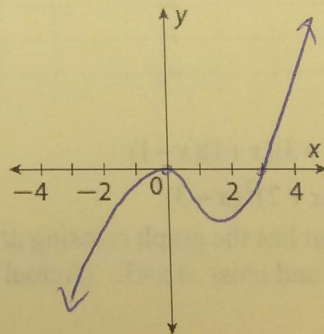
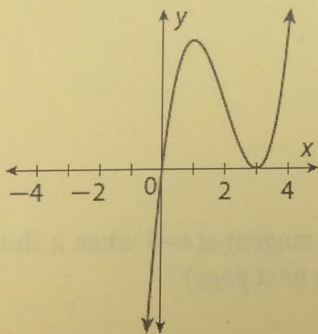


$x = -2, 2$

$$f(x) = -x(x-2)(x+2)(x-4)$$

$$f(x) = -(x+2)^2(x-2)^2$$

19. **Explain the Error** A student was asked to sketch the graph of the function $f(x) = x^2(x-3)$. Describe what the student did wrong. Then sketch the correct graph.



The student has the graph crossing at $x=0$ and tangent at $x=3$ when it should be tangent at $x=0$ and cross at $x=3$.