

Solving Radical Equations

Solve each rational equation algebraically:

1. $\frac{x}{x+4} = -3$

Cross Multiply

2. $\frac{x}{2x-10} = \frac{3}{2(x-5)}$

$x \neq 5$

$$1(x) = 3(2x-10)$$

$$x = 6x - 30$$

$$0 = 5x - 30$$

$$+30 \quad +30$$

$$\frac{30}{5} = \frac{5x}{5}$$

$$x = 6$$

3. $\frac{9}{4x} - \frac{5}{6} = -\frac{13}{12x}$

4. $\frac{3}{x+1} + \frac{2}{7} = \frac{2}{1}$

$x \neq -1$

Kill the Denominator

LCD: 7(x+1)

$$\frac{3}{(x+1)} \cdot \frac{7}{7} + \frac{2}{7} \cdot \frac{(x+1)}{(x+1)} = \frac{2}{1} \cdot \frac{7(x+1)}{7(x+1)}$$

$$21 + 2x+2 = 14x+14$$

$$\frac{23}{14} = \frac{12x+14}{-14}$$

$$\frac{9}{12} = \frac{12x}{-12}$$

$$x = \frac{9}{12} = \left(\frac{3}{4}\right)$$

5. $\frac{56}{x^2 - 2x - 15} - \frac{6}{x+3} = \frac{7}{x-5}$

7. $\frac{5}{2x+6} - \frac{1}{6} = \frac{2}{x+4}$

$x \neq -3, -4$

LCD: $2 \cdot 3(x+3)(x+4)$

$$\frac{5}{2(x+3)} \cdot \frac{3(x+4)}{3(x+4)} - \frac{1}{6} \cdot \frac{(x+3)(x+4)}{(x+3)(x+4)} = \frac{2}{(x+4)} \cdot \frac{2 \cdot 3}{2 \cdot 3}$$

$$15x+60 - x^2 - 7x - 12 = 12x+36$$

$$-x^2 + 8x + 48 = 12x + 36$$

$$0 = x^2 + 4x - 12$$

$$0 = (x+6)(x-2)$$

$$x = -6, 2$$

8. $\frac{5}{x^2 - 3x + 2} - \frac{1}{x-2} = \frac{x+6}{3x-3}$

- 16. Art** A glassblower can produce several sets of simple glasses in about 3 hours. When the glassblower works with an apprentice, the job takes about 2 hours. How long would it take the apprentice to make the same number of sets of glasses when working alone?

- 17.** Kelsey is kayaking on a river. She travels 5 miles upstream and 5 miles downstream in a total of 6 hours. In still water, Kelsey can travel at an average speed of 3 miles per hour. What is the average speed of the river's current?

$$d = r \cdot t \quad t = \frac{d}{r} \quad \text{LCD: } (3-x)(8+x)$$

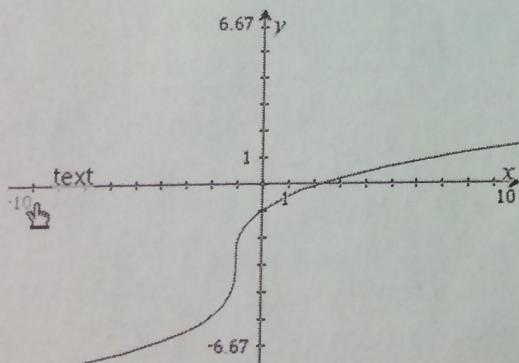
$$\boxed{\text{River speed} = 2 \text{ mph}}$$

$$\frac{(3+x)}{(3+x)} \cdot \frac{5}{3-x} + \frac{5(8-x)}{(3+x)(3-x)} = \frac{5(3+x)(8-x)}{(3+x)(3-x)}$$

$$\begin{aligned} 15 + 5x + 15 - 5x &= 6(9 - x^2) \\ 30 &= 54 - 6x^2 \\ +6x^2 - 54 &= -54 + 6x^2 \\ 6x^2 - 24 &= 0 \quad (x^2 - 4) = 0 \quad x = -2, 2 \\ 6(x^2 - 4) &= 0 \quad (x+2)(x-2) = 0 \\ 6 & \end{aligned}$$

Review

1. Write an equation to represent
the graphed function



2. Graph the function $g(x) = \sqrt{\frac{1}{5}(x+2)} - 2$

