

Defining and Evaluating Logarithms

Write the following in logarithmic form.

1.  $5^3 = 125$

$\log_5 125 = 3$

2.  $3^3 = 81$

3.  $4^3 = x$

$\log_4 x = 3$

4.  $10^5 = 100000$

5.  $e^4 \approx 54.6$

$\ln 54.6 \approx 4$

Write the following in exponential form.

6.  $\log_6 1296 = 4$

7.  $\log_8 x = y$

~~8~~  $8^y = x$

8.  $\log_2 x = 5$

9.  $\ln 5 \approx 1.6$

10.  $\log 1,000,000 = 6$

$e^{1.6} \approx 5$

11. If  $f(x) = \log_3 x$ , find  $f(243)$  and  $f(2187)$

$f(243) = \log_3 243 = \boxed{5}$       $3^5 = 243$

$f(2187) = \log_3 2187 = \boxed{7}$       $3^7 = 2187$

12. If  $f(x) = \log_6 x$ , find  $f(36)$  and  $f(1296)$

13. Find the exact value of the following:

(a)  $\log_2 8 = x = \boxed{3}$

$$2^x = 8$$

$$2^3 = 8$$

b.  $\log_5 625 =$

Use a scientific calculator to find the common logarithm and the natural logarithm of the given number. Verify each result by evaluating the appropriate exponential expression.

16. 19

$\ln(x)$

(17.) 9

$\log(9) = 0.95$
$\ln(9) = 2.20$

18. 0.6

(19.) 0.31

$\log(0.31) = -0.51$
$\ln(0.31) = -1.17$