

Solve the following equations graphically. Find the intersection

1. $4e^{0.1x} = 60$

2. $120e^{2x} = 75e^{3x}$

3. $5 = 625e^{0.02x}$

Window: y_1 y_2
 $x_{min}=0$ $y_{min}=250$ $x=0.47$
 $x_{max}=1$ $y_{max}=350$

Solve the following equations algebraically

get log alone or get exponent alone. Take inverse.

4. $\frac{7e^{3x}}{7} = \frac{42}{7}$

5. $5^{2x} = 15$

$\ln e^{3x} = \ln 6$

$\frac{3x}{3} = \frac{\ln(6)}{3} = 0.60$

6. $\log_{10} x^2 = 4$

7. $\ln(x-3) = 4 \ln 2$

$\sqrt{x^2} = \sqrt{10^4}$

$x = \sqrt{10000} = 100$

8. $2^x - 6 = 10$
 $+6 +6$

9. $\log_4(x-5) = -1$

$\log_2 2^x = \log_2 16$

$x = \log_2(16) = 4$

$x=4$

10. The price P of a gallon of gas after t years is given by the equation $P = P_0(1+r)^t$ where P_0 is the initial price of gas and r is the rate of inflation. If the price of a gallon of gas is currently \$3.25, how long will it take for the price to rise to \$4.00 if the rate of inflation is 10.5%?

\uparrow P_0
 r (change to decimal)

Price initial price rate of \uparrow
 • get exponent alone
 • take log

$$4.00 = 3.25(1+.105)^t \Rightarrow \frac{4}{3.25} = \frac{3.25(1.105)^t}{3.25}$$

$$t = \log_{1.105} \left(\frac{4}{3.25} \right) = \boxed{2.1 \text{ years}}$$

11 Match the equations with the solutions.

a. $9e^{3x} = 27$ _____ $x \approx 1.099$

b. $9e^x = 27$ _____ ~~$x \approx 1.022$~~ $x \approx 0.341$

c. $9e^{3x-4} = 27$ _____ $x \approx 0.366$

d. $9e^{3x} + 2 = 27$ _____ $x \approx 1.700$

Hints:

a) $\frac{9e^{3x}}{9} = \frac{27}{9}$

~~$\ln(e)^{3x}$~~ $\ln(3)$

$3x = \ln(3)$

$x = \frac{\ln(3)}{3} =$

b) $\frac{9e^x}{9} = \frac{27}{9}$

~~$\ln(e)^x$~~ $\ln(3)$

$x = \ln(3) =$

c) $9e^{3x-4} = 27$

d) $9e^{3x} + 2 = 27$