9 Starts 
$$w/2$$
 2-10 50 -250 1250 ends  $w/-6250$   $y=-5$   $1-6250$ 

## 8-3 Exponential Review

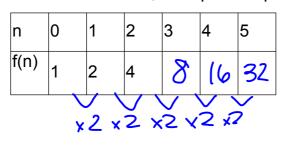
I can apply exponential properties and use them
I can model real-world situations using exponential functions

#### **GET A CALCULATOR!!!!**

#### Warm-Up

1. Find the next three terms in the sequence

2. Fill in the table, then plot the points (label your scale)



If we connected the points, what do you notice about the graph?

Have you ever seen a graph like this before?

# **EXPONENTIAL FUNCTION**

$$f(x) = a(b)^{x} - Exponent$$
Initial Value Base
(y-intercept) (Multiplier)

Starting

Graph the following functions on a calculator and sketch. Be sure to plot the y-intercept

a. 
$$f(x) = 2^x$$
 b.  $f(x) = \left(\frac{1}{2}\right)^x$ 

What did you notice about the graphs and their equations?

### **Exponential Growth and Decay**

Bigger than 
$$f(x) = a(b)^x$$

Bigger than  $f(x) = a(b)^x$ When b>1, the function represents exponential growth

When (0 < b < 1), the function represents **exponential decay** 

Determine whether each function represents growth or decay

a. 
$$f(x) = 13 \left(\frac{1}{3}\right)^x$$

$$\frac{1}{3} 2 \int_{1}^{2} Decay$$

b. 
$$g(x) = \left(\frac{3}{2}\right)^x$$

$$\frac{3}{2} > 1 \quad \text{Growth}$$

Write one equation that represents growth and one that represent decay

# **Exponential Growth/Decay Equation**

$$f(t) = a(1 \pm r)^{t}$$

- = decreasing

f(t): amount after time (t)

a: initial amount

r rate (% as a decimal)

t: time (variable)

John researches a baseball card and find that it is currently worth \$3.25. However, it is supposed to increase in value 11% per year.  $f(t) = a(1 \pm r)^t$ 

a) Write an exponential equation to represent this situation

$$a = \$3.25$$
  
 $r = .11$   
b) How much will the card be worth in  $(10)$  years?

c) Use your graphing calculator to determine in how many years will the card be worth (\$26)

$$3.25(1.11)^{t} = 26$$

#### You Try!

On federal income tax returns, self employed people can depreciate the value of business equipment. Suppose a computer valued at \$2765 depreciates at a rate of 30% per year.  $f(t) = a(1 \pm r)^t$ 

- a) Write an exponential equation to model this situation  $f(t) = 2765 (1 .30)^{t} = 2765 (0.7)^{t}$
- b) How much will this computer be worth in 5 years?

$$f(s) = 2765(.7)^{s} = $464.71$$

c) Use your graphing calculator to determine in how many years will the computer be worth \$350.

$$2765(.7)^{t} = 350$$
  
 $y_{1}$   $y_{2}$   
 $t = 5.8$  years

The population of Orem in 1950 was 4,000 and was increasing at a rate of 2.6% per year.

a) Predict the population of Orem in 1975 and 2000.

b) Using your graphing calculator, predict when Orem's population will hit 200,000 people.

The half-life of Carbon-14 is 5700 years. If a fossil decayed from 15 grams to 1.875 grams, how old is the fossil? (use your calculator)

#### **Compound Interest Formula**

$$A(t) = P\left(1 + \frac{r}{n}\right)^{e}$$

P is the principal (Starting amount)

r is the annual interest rate - % as decimal

n is the number of compounding periods per year t is the time in years

annually: n=1 Semi-annually: 2=n

monthly
n=12

# Write an equation then find the final amount for each investment.

a. \$1000 at 8% compounded semiannually for 15 years

$$A(t) = P\left(1 + \frac{r}{n}\right)^{nt}$$

You Try!

b. \$1750 at 3.65% compounded daily for 10 years

Using a calculator, determine how many years it will take for the amount to reach \$4000.

Investigate the growth of \$1 investment that earns 100% annual interest (r=1) over 1 year as the number of compounding periods, n, increases.

Compounding schedule	n	$1\left(1+\frac{1}{n}\right)^n$	Value of A
annually	1		
semiannually	2		
quarterly	4		
monthly	12		
daily	365		
hourly	8760		
every minute	525600		

What does the value of A approach?

#### The value e is called the natural base

The exponential function with base e,  $f(x)=e^x$ , is called the natural exponential function.

$$e \approx 2.71828182827$$

what you need to know is  $e \approx 2.7$ 

Evaluate 
$$f(x) = e^x$$
 for

a. 
$$x = 2$$

b. 
$$x = \frac{1}{2}$$

c. 
$$x = -1$$

Many banks compound the interest on accounts daily or monthly. However, some banks compound interest continuously, or at every instant, by using the *continuous compounding formula*.

#### **Continuous Compounding Formula**

If *P* dollars are invested at an interest rate *r*, that is compounded continuously, then the amount, *A*, of the investment at time *t* is given by

$$A(t) = Pe^{rt}$$

A person invests \$1550 in an account that earns 4% annual interest compounded continuously.

- a. Write an equation to represent this situation
- b. Using a calculator, find when the value of the investment reaches \$2000.

$$A(t) = Pe^{rt}$$

An investment of \$1000 earns an annual interest rate of 7.6%.

Compare the final amounts after 8 years for interest compounded quarterly and for interest compounded continuously.